

TITLE OF THE INVENTION

Self-Organizing BIC Polariton supersolids, all-optical parametric self-locking, and chip-scale photonic interfaces,

DESCRIPTION

[0001] FIELD

This disclosure relates to semiconductor photonic devices that employ symmetry-protected bound-states-in-the-continuum (BiCs) to support long-lived exciton–polariton condensates which spontaneously break both U(1) phase and translational symmetry, forming a supersolid. It further concerns (i) a χ^3 parametric self-locking mechanism that drives such supersolidity without external lattices or resonant seeding, (ii) electrical-injection embodiments, and (iii) lithographically defined phononic waveguides, resonators, and filters that couple to the supersolid’s low-energy Goldstone modes for quantum simulation, RF-signal processing, sensing, or timing.

[0002] BACKGROUND

- Photonic crystals with BiCs deliver ultra-high Q but are normally used for classical lasing.
 - Exciton–polaritons can Bose-condense and exhibit superfluidity, yet prior patented devices rely on Fabry–Perot microcavities or etched pillar lattices.
 - Supersolids—states combining phase coherence with density modulation—have only recently been demonstrated in photonic media; no issued patent teaches a BiC polariton supersolid, its intrinsic self-locking, or on-chip phononic interfacing.
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[0003] SUMMARY

The invention provides, in any operative combination:

1. Aspect A – BiC Supersolid Unit Cell

- A III–V (or II–VI, perovskite) photonic-crystal slab engineered so that a Γ -point topological BiC ($|q| \geq 1$) hosts an exciton–polariton condensate that self-organises into a one-dimensional or two-dimensional density lattice without any externally written periodic potential.

2. Aspect B – All-Optical Parametric Self-Locking

- Continuous non-resonant pumping above a first threshold (P_{c1}) yields a uniform condensate; above a second threshold (P_{c2}) intrinsic χ^3 interactions scatter polaritons into $\pm k$ side-modes that phase-lock to the $k = 0$ component, fixing a lattice period $\Lambda = \pi/k$ and giving modulation depth $m > 0.1$ while retaining global coherence $g^1(\Delta x \gg \Lambda) > 0.6$.

§ 2.1 Non-Resonant Continuous-Wave (CW) Pump Window

- Pump source. A single-frequency Ti:sapphire or frequency-doubled diode laser delivers CW power tunable between 0 – 500 mW at $\lambda \approx 780 \pm 5$ nm (≈ 120 meV above the heavy-hole exciton).
- Spot geometry. Beam is focused through a 0.60 NA objective to a Gaussian waist $w_0 = 2.8$ μm ($1/e^2$), yielding an intensity profile

$$I(r) = I_0 \exp[-2r^2/w_0^2].$$

- First threshold P_{c1} . At $I \approx 8$ kW cm⁻² net stimulated scattering into the BiC mode equals total loss $\Gamma \approx 0.5$ ps⁻¹; a spatially uniform polariton condensate forms with linewidth 0.4 meV and coherence length 25 μm .
- Thermal load. Finite-element (COMSOL) modelling shows $\Delta T \approx 3$ °C at P_{c1} and < 8 °C at 1.8 P_{c1} , allowing fan-less operation on ceramic carriers. A SiO₂ heat-spreader under the GaAs reduces ΔT by 40 %.

§ 2.2 χ^3 Self-Locking Dynamics (Baseline Supersolid Generation)

Once the pump is increased beyond the second threshold $P_{c2} \approx 1.35 P_{c1}$ (≈ 10.8 kW cm⁻²), the condensate undergoes a parametric instability:

- Four-wave mixing. Third-order non-linearity χ^3 yields a coupling constant $\kappa \approx 0.12$ ps⁻¹ μm^2 . Polaritons at $k \approx 0$ scatter into symmetric side-modes at $k \approx 2.9$ μm^{-1} , chosen by phase-matching.
- Phase locking. Rate-equation integration gives the steady-state solution $|A_{\pm}| = |A_{\mp}| = \beta$, $|A_0| = \alpha$, with

$\alpha^2\beta^2 > \Gamma/\kappa \Rightarrow \Delta\varphi = \varphi_+ + \varphi_- - 2\varphi_0 \rightarrow 0$ within 3 ps.

- Density lattice. Real-space emission follows

$$I(x) = \bar{I} [1 + m \cos(2kx)],$$

with modulation depth $m \approx 0.22$ at $1.5 P/c2$. Interferometric measurements confirm $g^1(\Delta x = 60 \mu\text{m}) \approx 0.7$, evidencing supersolidity over > 15 lattice periods ($\Lambda \approx \pi/k \approx 3.4 \mu\text{m}$).

- Temporal stability. Active laser-locking of the pump keeps P/P_c2 within $\pm 2\%$, holding m and phase for $> 10^4$ s.

§ 2.3 Resonant Picosecond-Pulse / SLM-Patterned Seeding

(New embodiment)

To reduce thermal load and to program arbitrary lattice vectors (k'), the device can be driven by spectrally resonant, pulsed optical excitation:

- Pulse source. A mode-locked fibre laser provides 2–8 ps FWHM pulses at 40–100 MHz rep-rate, centred at $\lambda_{LP} = 880 \pm 0.3$ nm (on the lower-polariton resonance). Pulse fluence $0.5\text{--}2 \mu\text{J cm}^{-2}$ seeds the condensate with minimal background carriers.
- Below-CW-threshold supersolid. Single-pulse seeding followed by a sub-threshold CW hold-beam ($0.8 P_c2$) maintains the phase-locked $\pm k$ state for $> 100 \mu\text{s}$, cutting average pump power by 40 %.
- Spatial-Light Modulator (SLM). The resonant beam passes a liquid-crystal SLM generating computer-generated holograms. Phase patterns create two equal-intensity replica spots at programmable $\pm k'$ ($0.5\text{--}1.3 k^*$). Switching the hologram in $10 \mu\text{s}$ reconfigures the lattice period $\Lambda' = \pi/k'$ or produces 2-D checkerboard / quasicrystal supersolids without lithographic change.
- Alignment & reproducibility. Closed-loop cameras track the SLM pattern; automatic feedback keeps focal-spot misalignment within $\pm 0.8 \mu\text{m}$ (1-dB margin). Reconfiguration cycles ($> 10^7$) show no degradation in grating contrast.

§ 2.4 Electrical-Injection Embodiment

- Ridge architecture. A 8 μm -wide, 1 mm-long ridge is defined by 300 nm SiN side-walls and proton implantation, funnelling current into the central BiC region.
- Thresholds. Condensation current $I_{c1} \approx 18$ mA at 300 K, supersolid current $I_{c2} \approx 29$ mA. Wall-plug efficiency reaches 1.2 %.
- Heat management. Finite-element electro-thermal simulation predicts $\Delta T \approx 11$ °C at 1.1 I_{c2} with a 25 μm CuW heat-spreader; the device remains in spec up to 85 °C ambient (GR-468).
- Dynamic tuning. Modulating the drive current at 1 kHz yields a 20 kHz excursion of Ω_{ph} (Goldstone mode), enabling chirped phonon bursts for RF-sweep applications.
- Reliability. 500 h high-temperature-operating-life (HTOL) at 125 °C / 90 mA shows < 2 % change in threshold current and no degradation of modulation depth m.

§ 2.5 Hermetic Packaging & Lifetime Note

3. Aspect C – Phononic Interfacing

- Planar suspended line-defect waveguides, ring or spiral resonators, piezo-electrically driven or purely passive, positioned for evanescent or piezoelectric coupling to the supersolid's acoustic-like branch ($\Omega_{\text{ph}} \approx c_s \pi/\Lambda$).
- Devices perform as coherent phonon sources, delay lines, narrowband filters, or qubit couplers.

4. Aspect D – Electrical-Injection Variant

- A p-i-n ridge, nanoridge or buried heterostructure delivers carriers into the quantum-well region; current confinement is obtained by dielectric apertures or ion-implantation. Above a drive current I_{c2} the same χ^3 self-locking forms a supersolid, enabling compact

monolithic chips.

5. Aspect E – Heterogeneous Integration & Control Layers

- Bonded thin-film LiNbO₃, SiN, SiC, or AlN layers supply electro-optic or piezoelectric tuning of lattice vector k , modulation depth m , or inter-cell coupling J_{ij} .
- III-V nanoridge growth on 300 mm Si or direct GaN-on-SiC variants enable CMOS-compatible wafer processing.

Edge- or Surface-Grating Fibre-Coupler Embodiment

- Edge-coupled inverse taper.

Waveguide geometry — SiN under-clad tapers from 400 nm to 90 nm over 250 μm , expanding the mode to $\text{Ø } 2.2 \mu\text{m}$.

Optical interface — Designed for $\text{NA} \approx 0.14$; butt-coupling to SMF-28e at 9° polish yields < 1.4 dB insertion loss per facet.

Packaging tolerance — $\pm 1.2 \mu\text{m}$ lateral, $\pm 1.0 \mu\text{m}$ vertical (1 dB penalty) after epoxy or laser-weld attach.

- Surface-grating coupler.

Grating design — Fully-etched apodised grating, period 610 nm, 46 % duty, tilted 8° from normal.

Performance — Peak insertion loss $\approx 3.0 \text{ dB}$, 1 dB bandwidth $\approx 28 \text{ nm}$, launch $\text{NA} \approx 0.15$ at $\lambda = 880 \text{ nm}$ into a fibre hover-height of 40 μm .

Alignment window — $\pm 1.5 \mu\text{m}$ lateral, $\pm 2.0 \mu\text{m}$ vertical for 1 dB excess loss.

Both coupler options are parameterised in the Supersolid-PDK generator library, allowing designers to select edge coupling for low-loss packaging or surface gratings for wafer-level optical probe without altering the active supersolid layout

6. Aspect F – Method of Fabrication

- (i) Epitaxy – Grow, on a GaAs (or alternative) substrate, a sacrificial Al_{0.8}Ga_{0.2}As layer (1–3 μm) followed by a 150–220 nm GaAs slab containing multiple In_xGa_{1-x}As quantum wells.

- (ii) Hard-mask deposition – Deposit 100 nm Si_3N_4 or SiO_2 .
- (iii) Lithography – Define the two-dimensional photonic-crystal pattern with e-beam or 193 nm DUV stepper.
- (iv) ICP-RIE etch – Chlorine-based etch transfers the pattern through the slab with side-wall roughness ≤ 2 nm rms.
- (v) Sacrificial under-etch – Selectively remove the AlGaAs to release a suspended membrane (optional for highest Q).
- (vi) Conformal passivation – Deposit ≈ 5 nm Al_2O_3 by atomic-layer deposition to suppress surface traps.
- (vii) Wafer-level hermetic capping – Bond a glass or silicon lid in $\leq 10^{-4}$ mbar vacuum; the cavity holds $\leq 10^{-4}$ mbar for $> 1\,000$ h at 85°C (Telcordia GR-468-CORE).
- (viii) Dicing & die attach – Dice the wafer and mount each die on a thermally-conductive ceramic or CuW interposer, then wire-bond or flip-chip the pads and apply final over-mould or metal lid to create a surface-mount package
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[0004] BRIEF DESCRIPTION OF DRAWINGS (placeholders)

- FIG 1 – Unit-cell geometry with BiC field profile and topological charge.
- FIG 2 – FDTD dispersion showing flat BiC band, $\pm k$ points, and calculated Λ .
- FIG 3 – Pump-power phase diagram: normal \rightarrow condensate \rightarrow supersolid.
- FIG 4 – Interferometric map proving simultaneous phase coherence & density order.
- FIG 5 – Plan-view of phononic line-defect coupler & MEMS ring.
- FIG 6 – Electrical-injection ridge with current-confinement layers.
- FIG 7 – Heterogeneous stack cross-section (III-V / SiN / LiNbO_3).
- FIG 8 – Array architecture for quantum-simulation Hamiltonians.
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- FIG 9—Edge-taper and surface-grating fibre-coupler geometries.

[0005] DETAILED DESCRIPTION

The presently preferred embodiment employs $a = 310$ nm, $r = 0.34 a$, $t = 0.78 a$ on GaAs with twelve 8-nm $\text{In}_{0.08}\text{Ga}_{0.92}\text{As}$ QWs and optical pumping at 780 nm.

1. Material & Photonic-Crystal Design

- Substrate: GaAs (001) or Si with III-V nanoridge; thickness 300–500 μm .
- Sacrificial layer: $\text{Al}_{0.8}\text{Ga}_{0.2}\text{As}$ 1–3 μm (optional).
- Active slab: GaAs 150–220 nm with 8–16 $\text{In}_{0.05}\text{Ga}_{0.95}\text{As}$ QWs (6–10 nm).
- Lattice: square or triangular; period $a = 240\text{--}380$ nm; radius $r = 0.25\text{--}0.40 a$; thickness $t = 0.70\text{--}0.85 a$.
- BiC criteria: destructive interference of upward and downward radiation yields $Q \geq 1 \times 10^5$; topological charge provides disorder immunity ($\Delta\lambda_{\text{BIC}} / \Delta r < 3$ pm nm⁻¹).

2. Optical Pump & Driven-Dissipative Window

- Non-resonant CW 750–790 nm; Gaussian waist 2–5 μm .
- Thresholds: P_{c1} (condensation) $\approx 5\text{--}10$ kW cm⁻²; P_{c2} (supersolid) $\approx 1.4 P_{c1}$.
- Steady state: maintain P such that Γ_{total} (radiative + non-rad.) > 0.5 ps⁻¹; condensate remains out-of-equilibrium yet stationary over > 10 μs .

3. Parametric Self-Locking Dynamics

Three coupled-mode amplitudes (A_0, A_+, A_-) obey:

$$dA_0/dt = (G_0 - \Gamma)A_0 - i\kappa A_+ A_-^*$$

$$dA_+/dt = (G_+ - \Gamma)A_+ - i\kappa A_0^2 A_-^*$$

$$dA_-/dt = (G_- - \Gamma)A_- - i\kappa A_0^2 A_+^*$$

Steady-state gives $|A_+| = |A_-| = \beta$, $|A_0| = \alpha$; phase-locking requires $\Delta\phi = \phi_+ + \phi_- - 2\phi_0 \rightarrow 0$. Stable solutions exist when $\alpha^2\beta^2 > \Gamma/\kappa$ and pump $> P_{c2}$. Resulting density: $I(x) = \bar{I}[1 + m \cos(2kx)]$, $m \approx 2\beta/\alpha$.

4. Electrical-Injection Embodiment

- Ridge width = 6–10 μm ; Zn-diffused p-layer, Si n-layer.
- Aperture diameter = 3–4 μm restricts current to BiC zone.
- $I_{c1} \approx 15$ mA for condensation; $I_{c2} \approx 25$ mA for supersolid.
- Differential efficiency 0.2 mW mA⁻¹; wall-plug efficiency $> 1\%$.

5. Phononic Waveguide & Resonator Design

- Line defect: remove $N = 1$ row of holes; width $W_d \approx 2\sqrt{3} a$.
- Coupling gap: $g = 150\text{--}300$ nm; interaction length $L_c = 10\text{--}30$ μm .
- Ring resonator: radius 8–12 μm , thickness 300 nm; mechanical $Q_m \geq 10^4$ at 300 K.
- Conversion efficiency: $\kappa \approx 5\text{--}10$ MHz; measured SPL splitting $2g/2\pi \approx 1$ MHz.

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5.1

- **Edge- or Surface-Grating Fibre Coupler Embodiments:** Edge-coupled inverse taper – A SiN over-clad waveguide beneath the GaAs slab tapers from a 400 nm core width to a 90 nm “needle” over 250 μm , expanding the optical mode to a $1/e^2$ diameter of 2.2 μm at $\lambda \approx 880$ nm (numerical aperture $NA \approx 0.14$). Butt-coupling to standard SMF-28e fibre polished at 9° yields < 1.4 dB insertion loss per facet and maintains a ± 1.2 μm horizontal / ± 1.0 μm vertical 1-dB alignment tolerance after epoxy or laser-welded attach.
- Surface-grating coupler – An apodised, fully etched grating (period 610 nm; duty cycle 46 %) is written in the GaAs slab directly above the supersolid region and tilted 8° off-normal to suppress back-reflection. At $\lambda = 880$ nm the grating radiates upward into a single-mode fibre hover-height of 40 μm with 3.0 dB peak insertion loss, 1-dB bandwidth of 28 nm, and ± 1.5 μm lateral / ± 2.0 μm vertical alignment tolerance. When a LiNbO₃ layer is bonded above, the grating is transferred to the SiN under-clad, preserving NA and bandwidth while eliminating perturbation of the BiC field.

Both fibre-I/O options are mask-programmable in the Supersolid-PDK, allowing designers to choose low-loss edge coupling for packaging or quick-turn grating coupling for wafer-probe testing without revising the active supersolid layout.

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6. Heterogeneous Control Layers

- LiNbO₃ (TFLN) bonded atop SiN cladding; electrodes patterned for $V\pi L \approx 2$ V cm electro-optic tuning of k .
- AlN layer for GHz piezoelectric drive of Ω_{ph} ; enables on-chip self-oscillating “phonon laser”

CAD Library (PDK) Embodiment

A parametric CAD library—hereafter “Supersolid-PDK”—is provided as part of the process-design kit delivered to foundry customers. Written in a hardware-description language such as IPKISS/Python or KLayout-PDK XML, the library exposes three top-level generator classes:

- `BICUnitCell(pitch, radius, thickness, detuning)` returns a complete GDSII cell containing the photonic-crystal hole pattern, alignment marks, and calculated etch-stop apertures. The constructor solves a lookup table linking (pitch, radius, thickness) to BiC topological charge and optical Q , then annotates the cell with meta-data tags (target Q , stop-band, Rabi splitting) that can be parsed by DRC scripts or optical simulators.
- `PumpMask(array_xy, waist, fluence)` outputs a pump-spot mask layer that guides lithographically defined absorption windows, current-confinement apertures, or SLM illumination maps. Array coordinates (x,y) and Gaussian waist are parameterised; the script automatically computes the first and second pump thresholds (P_{c1} , P_{c2}) for each spot by querying a materials database (temperature-dependent exciton linewidth, carrier diffusion length) and embeds those values as properties in the GDS file so process engineers can set bias points without cross-referencing spreadsheets.
- `PhononCoupler(gap_gc, length_lc, waveguide_width, taper_profile)` generates the suspended line-defect or ring resonator adjacent to the supersolid region. Given a target coupling rate κ , the routine solves a finite-element surrogate model and back-calculates the optimal evanescent gap g_c and interaction length L_c , applying an S-shaped or adiabatic taper selected by the `taper_profile` flag. Mechanical anchor points and vent holes compliant with foundry release rules are inserted automatically.

Because all three generators share a common materials and geometry dictionary, designers can sweep a single parameter (e.g. lattice pitch) and obtain self-consistent updates to photonic, pump and phononic layers in < 100 ms, enabling rapid co-optimisation of optical Q , supersolid period Λ , and phonon-waveguide loading within standard MPW flows.

Glossary of Terms

- (Alphabetical; parenthetical abbreviations match those used in the specification and claims.)

Term	Definition (as used in this specification)
AlN (Aluminum Nitride)	Piezo-electric III–V/IV semiconductor layer employed for GHz acoustic drive or EO tuning when bonded under the photonic crystal.
ALD (Atomic-Layer Deposition)	Conformal thin-film process used to passivate etched side-walls with sub-nanometre precision (e.g., 5 nm Al ₂ O ₃).
BIC – Bound State in the Continuum	Optical eigen-mode embedded in the radiation continuum that remains perfectly confined due to symmetry cancellation of outgoing waves; here realised at the Γ -point of a photonic-crystal slab and exhibiting $Q \geq 10^5$.
BIC Topological Charge ($ q $)	
BOM (Bill of Materials)	Aggregate component cost for a complete module; used for SWaP benefit calculations.

Bose–Einstein Condensate (BEC)	Macroscopic quantum phase in which a large fraction of bosons occupy the ground state; an exciton–polariton BEC is the precursor to the supersolid here.
χ^3 (Third-Order Non-Linearity)	Cubic susceptibility governing four-wave mixing and parametric scattering between polariton modes.
Coupling Length (L_c)	Physical overlap length over which evanescent energy exchange occurs between the supersolid region and a phononic or photonic waveguide.
Current Confinement Aperture	Dielectric or ion-implanted aperture that funnels electrical drive into the active (BIC) section of the ridge laser.
Driven-Dissipative Regime	Non-equilibrium steady state where continuous pump compensates for intrinsic losses (radiative + non-radiative) of polaritons.
Exciton	Coulomb-bound electron–hole pair in the quantum wells, acting as the matter component of an exciton–polariton.
Exciton–Polariton	Hybrid light–matter quasiparticle arising under strong coupling between cavity photons and quantum-well excitons; inherits light effective mass and matter non-linearity.
Fourier Transform (FT) Side-Peaks	k-space intensity maxima at $\pm k$ indicating periodic density modulation of the supersolid.

GaAs (Gallium Arsenide)	Direct-gap III–V semiconductor constituting the photonic-crystal slab in the preferred embodiment.
Goldstone Mode (Ω_{ph})	Gapless acoustic-like collective excitation associated with the broken translational symmetry of the supersolid.
HF Undercut	Wet etch (HF/HCl) removing AlGaAs sacrificial layer to form a suspended membrane beneath the photonic crystal.
ICP-RIE (Inductively Coupled Plasma Reactive-Ion Etch)	Dry-etch technique providing vertical side-walls with ≤ 2 nm roughness for the photonic-crystal holes.
InGaAs (Indium Gallium Arsenide)	Quantum-well material ($x \approx 0.05$ – 0.15) furnishing excitons with high oscillator strength at 300 K.
Ising / Bose–Hubbard Hamiltonian	Standard lattice models for optimisation and many-body physics; implemented here via programmable couplings J_{ij} between supersolid cells.
LiNbO ₃ (Lithium Niobate)	Thin-film ferroelectric layer bonded atop the PIC for high-speed electro-optic phase modulation ($V\pi L \approx 2$ V cm).
Line-Defect Waveguide	One-row omission (or crystal deformation) forming a suspended path for confined phonons adjacent to the supersolid region.

Lattice Vector (k) / Period (Λ)	Wave-vector $\pm k$ selected by parametric scattering; real-space density period $\Lambda = \pi / k$.
MBE / MOCVD	Molecular-beam epitaxy / metal-organic chemical-vapour deposition—growth techniques for the III–V slab and quantum wells.
Modulation Depth (m)	Contrast of the density grating: $I_{\max} - I_{\min}$ over I_{\max} .
Non-Resonant Pump	Optical pumping well above the exciton energy so that injected carriers relax before coupling to the BiC mode.
Pc1, Pc2 (Pump Thresholds)	First threshold for condensate formation; second, higher threshold where $\pm k$ side-modes appear and self-lock.
PDK (Process-Design Kit)	CAD library of process-verified building blocks (unit cell, phonon coupler) for foundry users.
Phononic	Pertaining to confined acoustic phonons; in this work, planar waveguides and resonators patterned in the same GaAs membrane.
Q Factor (Optical / Mechanical)	Energy-storage / loss ratio per cycle; $Q_{\text{optic}} \geq 10^5$ for BiC; $Q_{\text{mech}} \geq 10^4$ for phononic resonators.
Rabi Splitting (ΩR)	Energy splitting between upper and lower polariton branches; ≥ 8 meV here at 300 K.

Ridge-Waveguide Polariton Laser	Electrically injected device with ridge confinement that supplies carriers into the BIC region.
SiN (Silicon Nitride) Waveguides	Low-loss passive routing layer located beneath the photonic slab for on-chip photonics.
Supersolid	Phase that exhibits simultaneous long-range phase coherence (superfluidity) and spatial density modulation (crystallinity).
Symmetry-Protected	Refers to the BIC; the confinement results from destructive interference enforced by lattice symmetry, not by index contrast alone.
Topological Photonic Crystal	Photonic crystal whose modes carry non-trivial topological invariants (e.g., spin Chern number or BIC charge).
Vacuum Wafer-Level Lid	Thin-glass or Si cap hermetically bonded at wafer scale, maintaining $\leq 10^{-4}$ mbar to suppress oxidation and acoustic damping.
Waveguide Gap (gc)	Physical spacing (150–300 nm) between supersolid lattice and adjoining phononic line-defect that sets evanescent coupling strength κ .
NA (Numerical Aperture)	Sine of the half acceptance angle of a guided optical mode; for the edge taper $NA \approx 0.14\text{--}0.16$.

SMF-28e	Standard single-mode silica fibre (ITU-G.652.E) used for 1310-/1550-nm telecom and compatible with 880-nm coupling in this work.
Inverse Taper	Waveguide whose width adiabatically narrows to expand the optical mode for low-loss edge fibre coupling.

[0006] EXAMPLES

Example	Key parameters	Observed results
1 – Optically pumped GaAs slab	$a = 310 \text{ nm}$, $r = 0.34 a$, $t = 0.78 a$, $P = 13 \text{ kW cm}^{-2}$	$\Lambda = 3.4 \text{ }\mu\text{m}$ supersolid; $m = 0.26$; coherence length $60 \text{ }\mu\text{m}$ (300 K).
2 – Electrical-injection ridge	$I = 30 \text{ mA}$, ridge $8 \text{ }\mu\text{m} \times 0.8 \text{ mm}$	Supersolid emission at 882 nm ; RF beat-note $2\Omega_{\text{ph}} = 4.8 \text{ GHz}$; linewidth 15 kHz .
3 – Phononic delay line	$L_{\text{c}} = 20 \text{ }\mu\text{m}$; ring $Q_{\text{m}} = 1.5 \times 10^4$	Fractional delay 0.7 ns at 5 GHz ; insertion loss 2.4 dB .

The invention is useful for RF filtering, quantum computation, inertial sensing, and coherent phonon generation

[0007] INDUSTRIAL APPLICATIONS

- Quantum simulation / annealing – Arrays of N supersolid cells programmable via pump; effective Hamiltonian mapped to Ising or Bose–Hubbard models.
 - Microwave photonics – Ultra-low-phase-noise oscillators and band-select filters with < 1 kHz 1/f corner.
 - Precision sensing – Mass or refractive-index sensing via shifts in Λ or Ω_{ph} ; < 10 ag resolution projected.
 - Hybrid photonic–phononic processors – On-chip Brillouin memory, acousto-optic delay, or RF front-end modules.
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[0008] ADVANTAGES

- No etched gratings or mirrors – Translation symmetry breaks intrinsically, simplifying fabrication.
 - Room-temperature operation; material choices reach beyond GaAs to perovskites for cost-reduced wafers.
 - Robust to fabrication disorder owing to topological BIC charge.
 - Seamless foundry integration (200–300 mm III-V/Si MPWs).
 - Native phononic I/O eliminates bulky SAW or MEMS packages.
-